

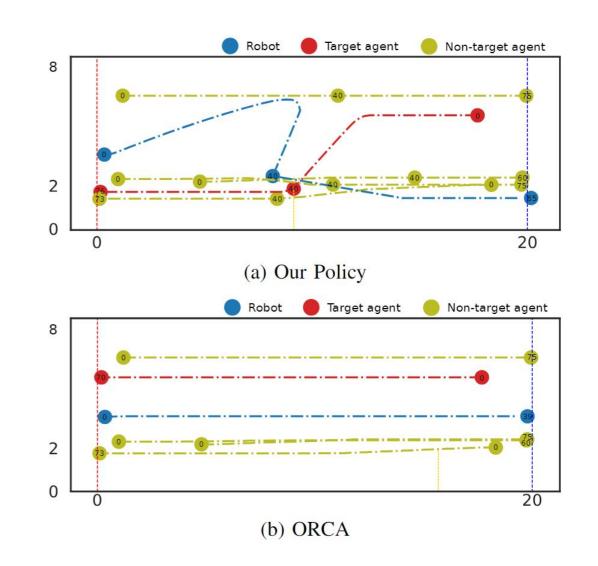
# I-ORCA – Implicitly Nudging Human Trajectories

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- Humans and robots are increasingly sharing the same physical space
- Past research has focused on designing collision-free trajectories for robots in crowded environments
- We envision a future where robots not only avoid collisions, but also actively guide them towards their objectives
- Such robots can help with crowd control, evacuation, tour guides, etc.





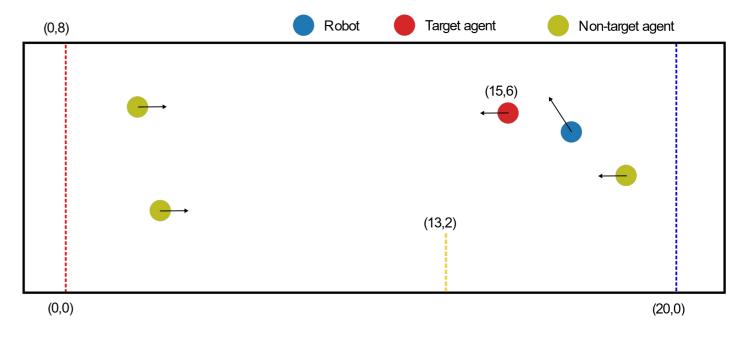
Social Navigation	<ul> <li>Design of robot policies that help them move smoothly in crowded environments</li> <li>Major focus on collision avoidance</li> <li>Performance measured through disturbance to human trajectories</li> </ul>

## Influencing Human Behavior

- Prior research focused on studying changes in human behavior due to robot behavior
- More recently, research has focused on designing robot behaviors that actively modify human behaviors



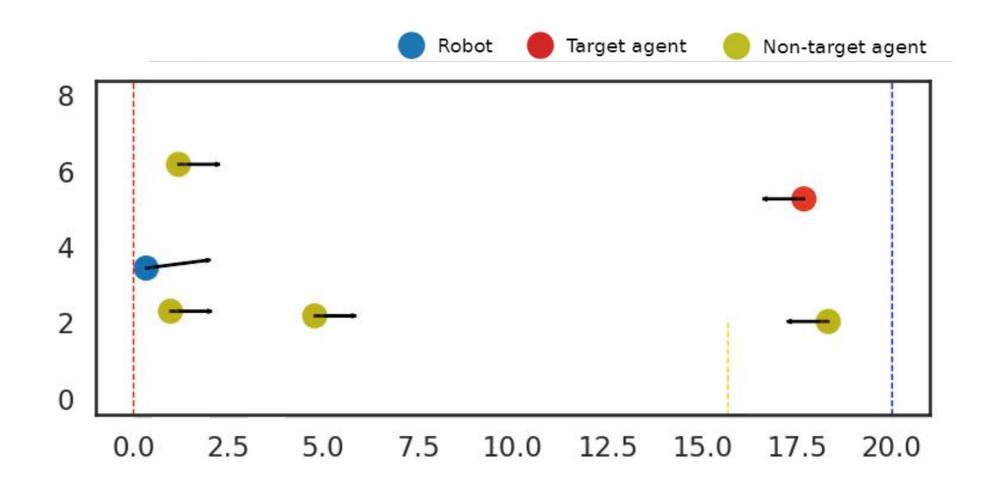
- We consider a hallway crossing scenario
- Each agent starts at one end of the hallway and moves towards the opposite end (red and blue dashed lines)
- The robot wants the target agent to reach the virtual goal line (gold dashed line)
- The virtual goal line is always 2m ahead of the target agent



Sample initial conditions



### **Illustrative example**



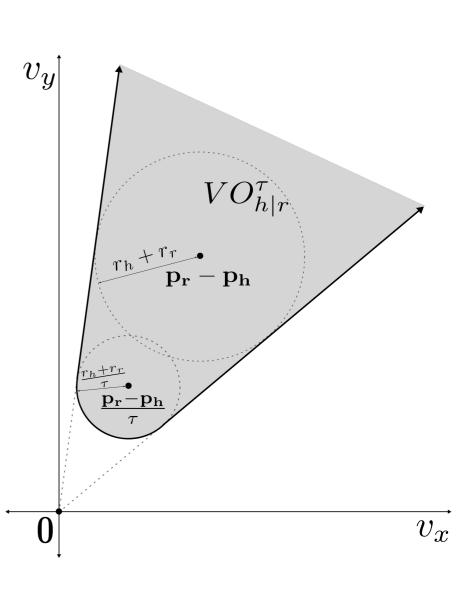
Results



- We leverage the idea that individuals will inherently try and avoid collisions when moving in a crowded environment
- We assume that this collision avoidance behavior is modeled using Optimal Reciprocal Collision Avoidance (ORCA)
- Under this assumption, we show that we can design a policy for a robot that can implicitly nudge a target agent toward a desired direction without affecting the other agents in the environment
- We also assume that all agents in the scene use ORCA with the same policy parameters
  - This assumption is made in all research dealing with ORCA since it is the only way to guarantee collision avoidance

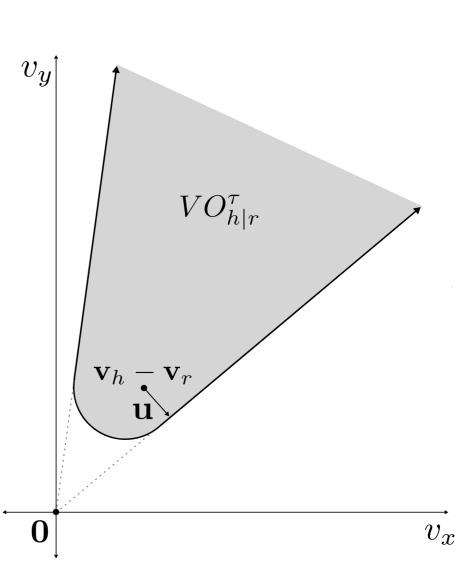


- Optimal Reciprocal Collision Avoidance (ORCA) works by using
  - Reciprocal Velocity Obstacles (RVOs) and,
  - the reciprocity assumption: Each agent shares the responsibility of avoiding collision
- For two circular agents h, r, if the relative velocity is outside the grey shaded region,
  - we can guarantee no-collisions in the next  $\tau$  timesteps if the agents continue with the same velocities





- If the relative velocity is within the gray region, collision can be avoided by modifying the relative velocity to be on the boundary of the velocity obstacle
- We project the relative velocity to the boundary and get *u*
- If the relative velocity becomes  $v_h v_r + u$ , we avoid collision in the next  $\tau$  timesteps
- In the original paper, the authors assumed that each agent equally shared the responsibility to avoid collisions
  - We modify this assumption by saying that each agent takes the full responsibility to avoid collision



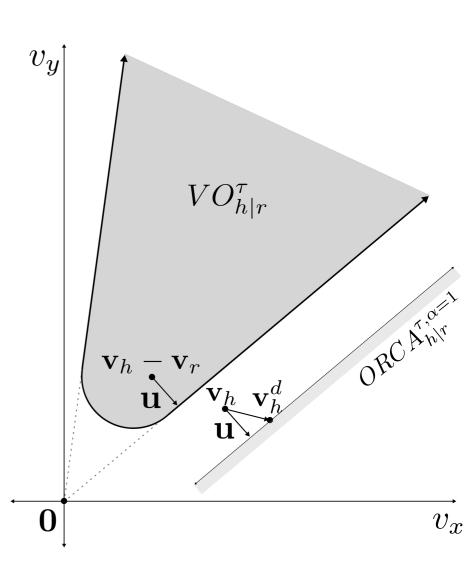




- Our key insight in this work is that
  - Agent r can set its velocity that nudges agent h's velocity towards a desired velocity
- Mathematically, this problem then becomes,

$$\min_{\mathbf{v}_r} ||\mathbf{v}_h^d - \mathbf{v}_h - \mathbf{u}||$$
  
s.t.  $\mathbf{u} = \operatorname{Proj}(\mathbf{v}_h - \mathbf{v}_r, \delta VO)$ 

 We can solve this problem geometrically, giving us the I-ORCA algorithm





### Algorithm 1: I-ORCA

**Data:**  $\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, r_h, r_r, \tau$  **Result:**  $\mathbf{v}_r$  $VO \leftarrow \text{GenerateVO}(\mathbf{p}_h, \mathbf{p}_r, r_h, r_r, \tau);$ 

 $v \in V \oplus (\mathbf{p}_h, \mathbf{p}_r, r_h, r_r, r),$   $overlap \leftarrow \text{CheckOverlap}(VO, \mathbf{v}_h, v_r^{max});$ if overlap then

 $\mathbf{u} \leftarrow \text{ComputeProjection}(VO, \mathbf{v}_h, \mathbf{v}_h^d);$  $\mathbf{v}_r \leftarrow \mathbf{v}_h + \mathbf{u} - \text{ChoosePoint}(VO);$ 

### else

$$\begin{vmatrix} \mathbf{u} \leftarrow \text{CloserToVO}(VO, \mathbf{v}_h, v_r^{max}); \\ \mathbf{v}_r \leftarrow \mathbf{v}_h + \mathbf{u}; \end{vmatrix}$$
end

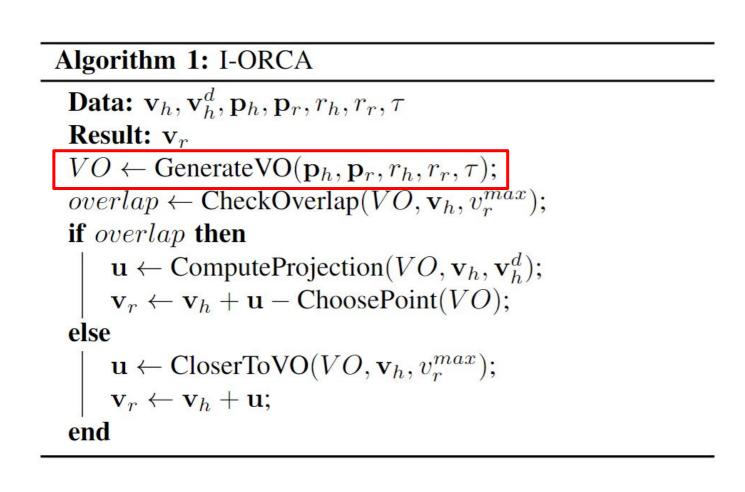
# $\mathbf{v}_h$ The velocity of agent h $\mathbf{v}_h^d$ The velocity of agent h $\mathbf{p}_h$ The desired velocity for agent h $\mathbf{p}_h$ The position of agent h $\mathbf{p}_r$ The position of agent r $r_h$ The radius of agent h $r_r$ The radius of agent r $\tau$ The planning time horizon

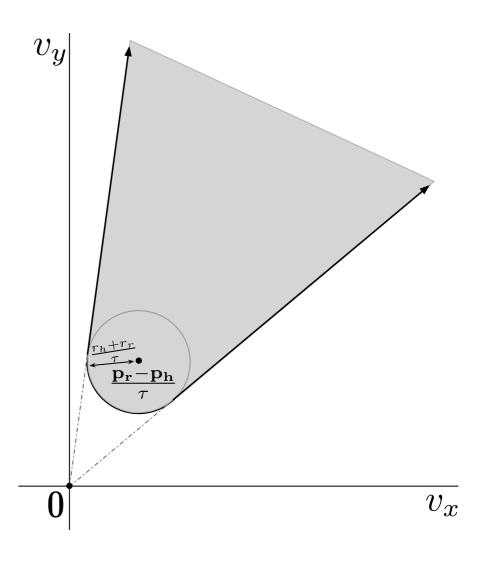
Description

Output Variable	Description
$\mathbf{v}_r$	The velocity for agent $r$

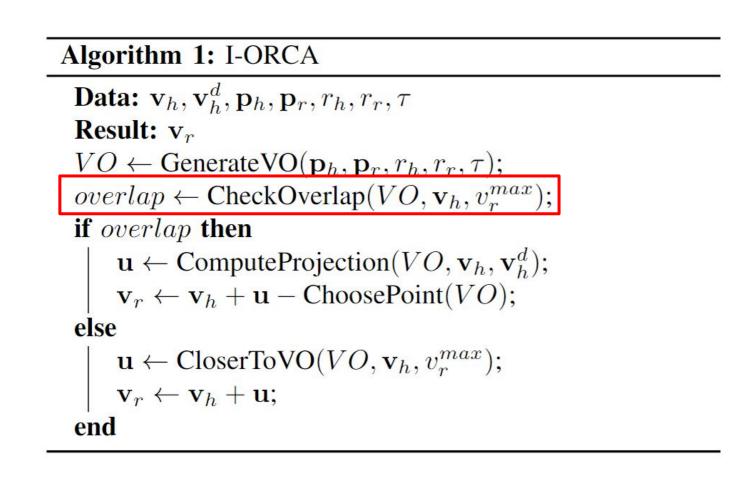
Input Variable

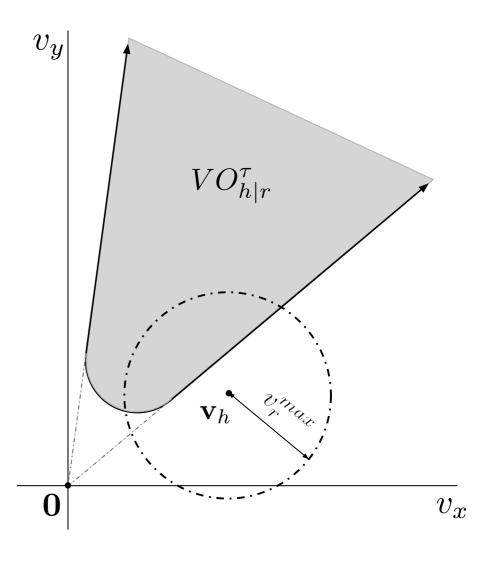




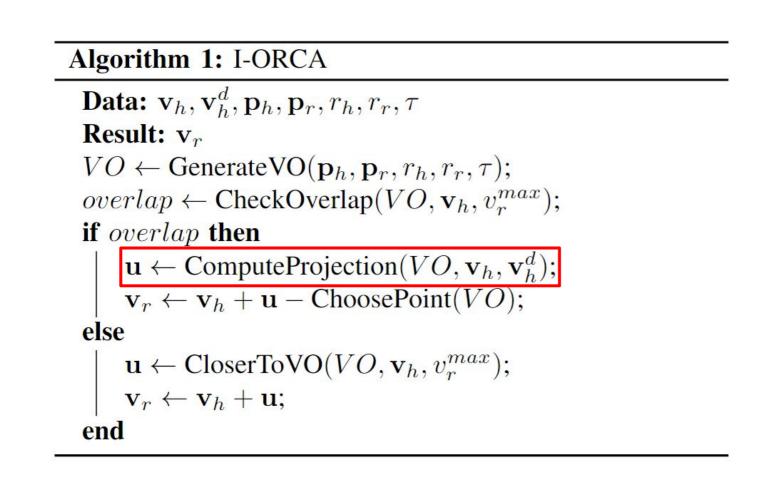


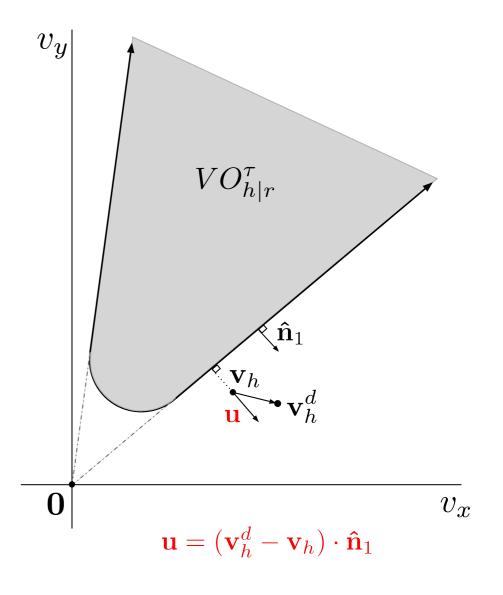




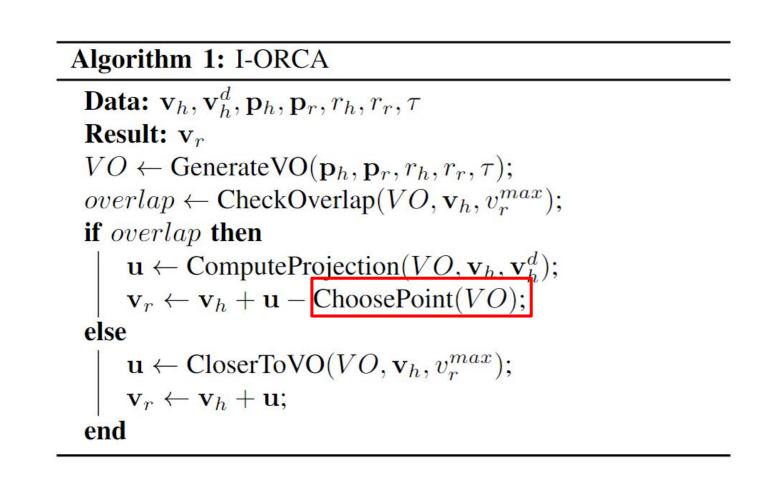


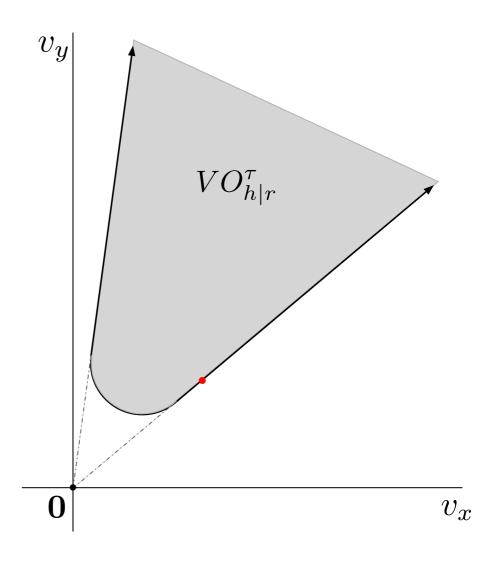




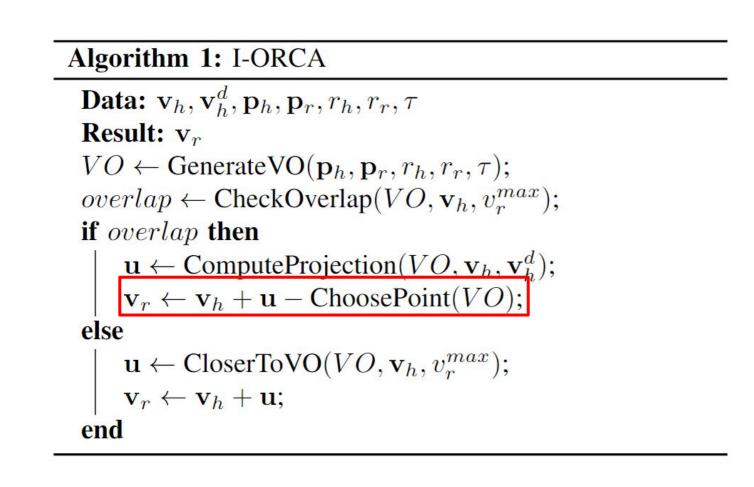


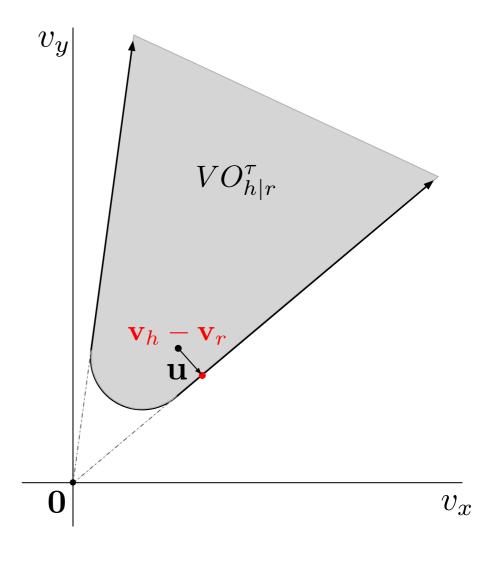




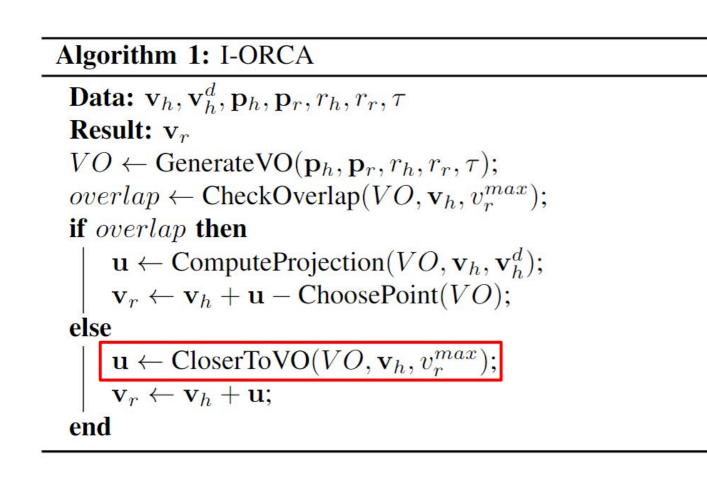


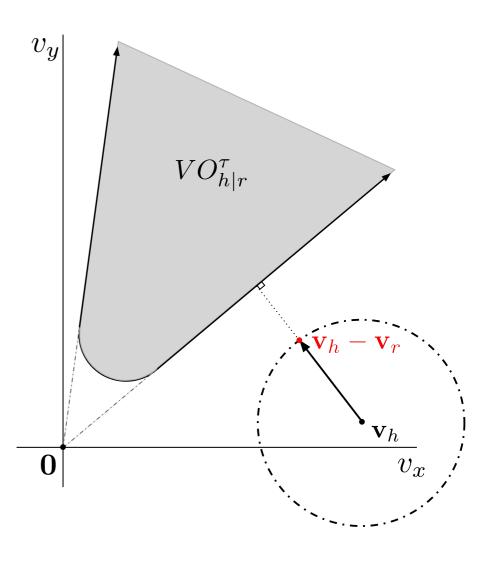






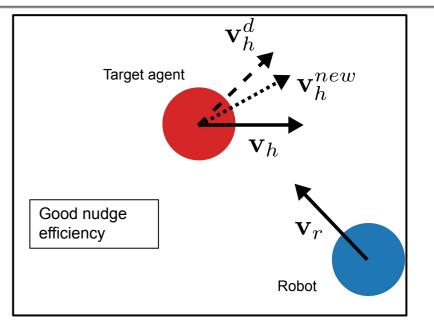


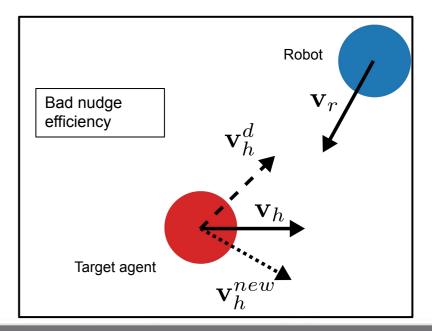






- Not all positions around the target agent are equally good at nudging it towards the desired direction
- Nudge efficiency is defined as the similarity between the target agent's new velocity after nudging to the desired velocity







1.00 3 0.95 2 0.90 Nudge efficiency > 0.85 -1 0.80 0.75 -2 2 3 > Relative velocities -3 -2 2

- The nudge efficiency was computed by
  - Sampling the robot's position around the target agent
  - Setting the robot's velocity using I-ORCA
  - Getting the target agent's velocity at the next time step using its motion model
  - Computing the cosine similarity between the desired velocity and the new velocity
- The illustration to the right shows the case when the target agent uses ORCA
- We see a similar plot when the target agent uses the social forces model



Algorithm 2: Smooth Efficient Nudge Policy		
<b>Data:</b> $\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, r_h, r_r, v_r^{max}, \tau$		
<b>Result:</b> $\mathbf{v}_r$		
$\mathbf{v}_r^I \leftarrow \text{I-ORCA}(\mathbf{Data});$		
$\mathbf{p}_c \leftarrow \text{ChoosePoint}(\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h);$		
if CheckConditions( $\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, \mathbf{p}_c$ ) then		
$\mathbf{v}_{r}^{pref} \leftarrow \mathbf{v}_{r}^{I};$		
$\mathbf{v}_r \leftarrow \text{ORCA}^n(\mathbf{v}_r^{pref}, \text{other agents' data});$		
else		
$\mathbf{v}_r^{pref} \leftarrow \text{VelocityTowards}(\mathbf{p}_c);$		
$\mathbf{v}_r^O \leftarrow ORCA^{n+1}(\mathbf{v}_r^{pref}, other agents' data);$		
$w_I \leftarrow \text{ComputeWeight}(\mathbf{p}_c, \mathbf{p}_r);$		
$\mathbf{v}_r \leftarrow w_I \mathbf{v}_r^I + (1 - w_I) \mathbf{v}_r^O;$		
end		

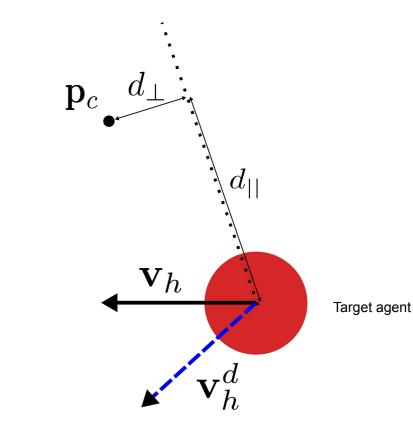
Input Variable	Description
$\mathbf{v}_h$	The velocity of agent $h$
$\mathbf{v}_h^d$	The desired velocity for agent $h$
$\mathbf{p}_h$	The position of agent $h$
$\mathbf{p}_r$	The position of agent $r$
$r_h$	The radius of agent $h$
$r_r$	The radius of agent $r$
au	The planning time horizon

Output Variable	Description
$\mathbf{v}_r$	The velocity for agent $r$



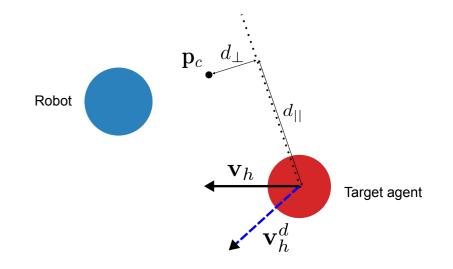
### **Smooth Efficient Nudging Policy**

Algorithm 2: Smooth Efficient Nudge Policy **Data:**  $\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, r_h, r_r, v_r^{max}, \tau$ **Result:**  $\mathbf{v}_r$  $\mathbf{v}_{r}^{I} \leftarrow \text{I-ORCA}(\mathbf{Data});$  $\mathbf{p}_c \leftarrow \text{ChoosePoint}(\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h);$ if *CheckConditions*( $\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, \mathbf{p}_c$ ) then  $\mathbf{v}_r^{pref} \leftarrow \mathbf{v}_r^I;$  $\mathbf{v}_r \leftarrow \text{ORCA}^n(\mathbf{v}_r^{pref}, \text{other agents' data});$ else  $\mathbf{v}_r^{pref} \leftarrow \text{VelocityTowards}(\mathbf{p}_c);$  $\mathbf{v}_r^O \leftarrow ORCA^{n+1}(\mathbf{v}_r^{pref}, other agents' data);$  $w_I \leftarrow \text{ComputeWeight}(\mathbf{p}_c, \mathbf{p}_r);$  $\mathbf{v}_r \leftarrow w_I \mathbf{v}_r^I + (1 - w_I) \mathbf{v}_r^O;$ end





**Algorithm 2:** Smooth Efficient Nudge Policy **Data:**  $\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, r_h, r_r, v_r^{max}, \tau$ **Result:**  $\mathbf{v}_r$  $\mathbf{v}_r^I \leftarrow \text{I-ORCA}(\text{Data});$  $\mathbf{p}_{c} \leftarrow \text{ChoosePoint}(\mathbf{v}_{h}, \mathbf{v}_{h}^{d}, \mathbf{p}_{h});$ **if** CheckConditions( $\mathbf{v}_{h}, \mathbf{v}_{h}^{d}, \mathbf{p}_{h}, \mathbf{p}_{r}, \mathbf{p}_{c}$ ) **then**  $\mathbf{v}_r^{pref} \leftarrow \mathbf{v}_r^I;$  $\mathbf{v}_r \leftarrow \text{ORCA}^n(\mathbf{v}_r^{pref}, \text{other agents' data});$ else  $\mathbf{v}_r^{pref} \leftarrow \text{VelocityTowards}(\mathbf{p}_c);$  $\mathbf{v}_r^O \leftarrow \text{ORCA}^{n+1}(\mathbf{v}_r^{pref}, \text{other agents' data});$  $w_I \leftarrow \text{ComputeWeight}(\mathbf{p}_c, \mathbf{p}_r);$  $\mathbf{v}_r \leftarrow w_I \mathbf{v}_r^I + (1 - w_I) \mathbf{v}_r^O;$ end



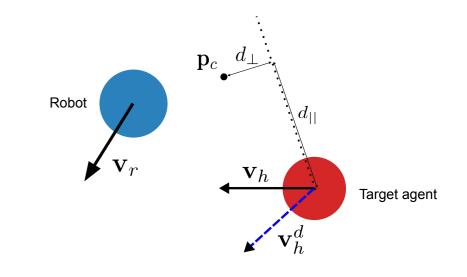
Checks the following conditions:

- The ego agent should be close to the point given by ChoosePoint
- 2. The ego agent must be on the same side of the boundary as the chosen point
- The ego agent's y-coordinate should be more than that of the target agent

**Note:** The third condition is context dependent. It works in our case since we want to nudge the target agent toward lower y-coordinates



Algorithm 2: Smooth Efficient Nudge Policy **Data:**  $\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, r_h, r_r, v_r^{max}, \tau$ **Result:**  $\mathbf{v}_r$  $\mathbf{v}_r^I \leftarrow \text{I-ORCA}(\mathbf{Data});$  $\mathbf{p}_c \leftarrow \text{ChoosePoint}(\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h);$ if  $CheckConditions(\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, \mathbf{p}_c)$  then  $\mathbf{v}_{r}^{pref} \leftarrow \mathbf{v}_{r}^{I};$  $\mathbf{v}_{r} \leftarrow \text{ORCA}^{n}(\mathbf{v}_{r}^{pref}, \text{other agents' data});$ else  $\mathbf{v}_r^{pref} \leftarrow \text{VelocityTowards}(\mathbf{p}_c);$  $\mathbf{v}_r^O \leftarrow \text{ORCA}^{n+1}(\mathbf{v}_r^{pref}, \text{other agents' data});$  $w_I \leftarrow \text{ComputeWeight}(\mathbf{p}_c, \mathbf{p}_r);$  $\mathbf{v}_r \leftarrow w_I \mathbf{v}_r^I + (1 - w_I) \mathbf{v}_r^O;$ end



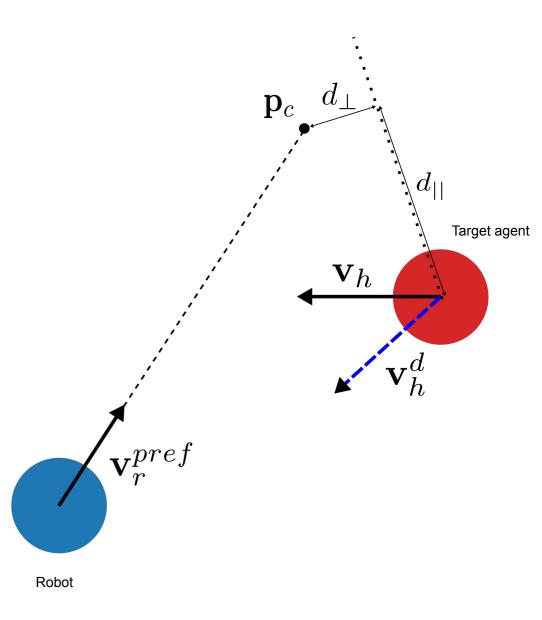
- Here, we nudge the target human
- Therefore, we select the robot's velocity using *ORCA<sup>n</sup>*, which only considers the non-target agents in planning

#### Caveat:

- This can lead to collisions between the robot and the target agent
- We saw collisions in <5% of the simulations we ran</li>
- Some policy parameters can be tuned to better avoid collisions

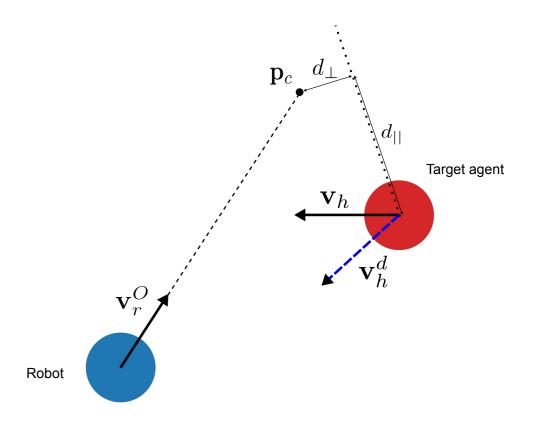


Algorithm 2: Smooth Efficient Nudge Policy **Data:**  $\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, r_h, r_r, v_r^{max}, \tau$ **Result:**  $\mathbf{v}_r$  $\mathbf{v}_r^I \leftarrow \text{I-ORCA}(\text{Data});$  $\mathbf{p}_c \leftarrow \text{ChoosePoint}(\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h);$ if  $CheckConditions(\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, \mathbf{p}_c)$  then  $\mathbf{v}_r^{pref} \leftarrow \mathbf{v}_r^I;$  $\mathbf{v}_r \leftarrow \text{ORCA}^n(\mathbf{v}_r^{pref}, \text{other agents' data});$ else  $\mathbf{v}_{r}^{pref} \leftarrow \text{VelocityTowards}(\mathbf{p}_{c});$  $\mathbf{v}_r^O \leftarrow ORCA^{n+1}(\mathbf{v}_r^{pref}, other agents' data);$  $w_I \leftarrow \text{ComputeWeight}(\mathbf{p}_c, \mathbf{p}_r);$  $\mathbf{v}_r \leftarrow w_I \mathbf{v}_r^I + (1 - w_I) \mathbf{v}_r^O;$ end





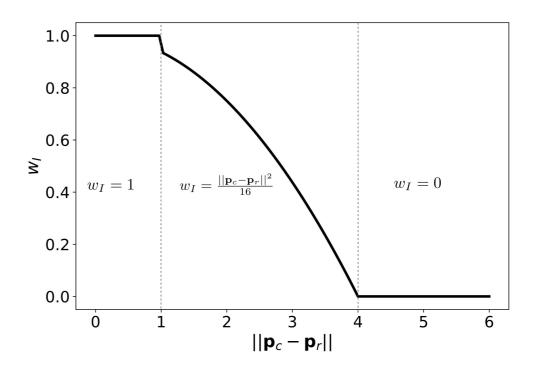
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- Here, we do not nudge the target human until we reach the efficient nudging region
- Therefore, we select the robot's velocity using  $ORCA^{n+1}$ , which considers all agents in the scene during planning



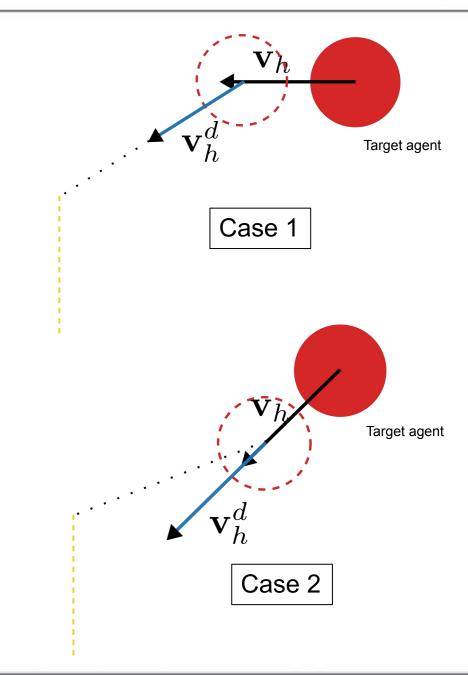
Algorithm 2: Smooth Efficient Nudge Policy **Data:**  $\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, r_h, r_r, v_r^{max}, \tau$ **Result:**  $\mathbf{v}_r$  $\mathbf{v}_r^I \leftarrow \text{I-ORCA}(\mathbf{Data});$  $\mathbf{p}_c \leftarrow \text{ChoosePoint}(\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h);$ if  $CheckConditions(\mathbf{v}_h, \mathbf{v}_h^d, \mathbf{p}_h, \mathbf{p}_r, \mathbf{p}_c)$  then  $\mathbf{v}_r^{pref} \leftarrow \mathbf{v}_r^I;$  $\mathbf{v}_r \leftarrow \text{ORCA}^n(\mathbf{v}_r^{pref}, \text{other agents' data});$ else  $\mathbf{v}_{r}^{pref} \leftarrow \text{VelocityTowards}(\mathbf{p}_{c});$  $\mathbf{v}_r^O \leftarrow \text{ORCA}^{n+1}(\mathbf{v}_r^{pref}, \text{other agents' data});$  $w_{I} \leftarrow \text{Compute Weight}(\mathbf{p}_{c}, \mathbf{p}_{r});$  $\mathbf{v}_{r} \leftarrow w_{I}\mathbf{v}_{r}^{I} + (1 - w_{I})\mathbf{v}_{r}^{O};$ end



Any non-increasing function of the distance between the ego agent and the chosen point should work here



- The desired velocity is set using the next position of the target agent, the virtual goal line, and the current velocity of the target agent
- First, the velocity with max speed is computed from the next anticipated position to the top of the virtual goal line
- If the y-component of this velocity is less than that of the target agent,
  - Set this velocity as the desired velocity
- Else,
  - Set the current velocity of the target agent as the desired velocity





### **Results - Nudge success**

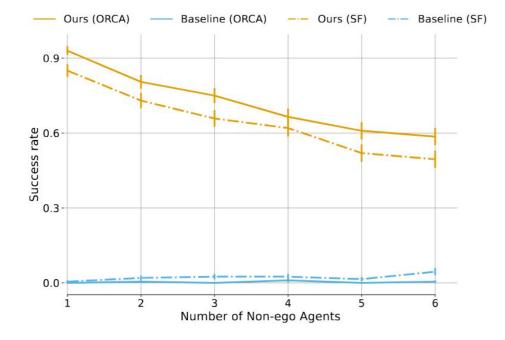


Fig. 6: Ratio of times the target agent reached the virtual goal line (SF - Social Force)

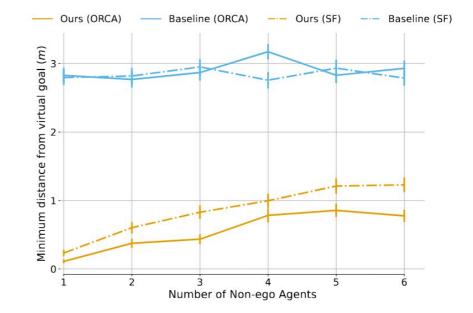
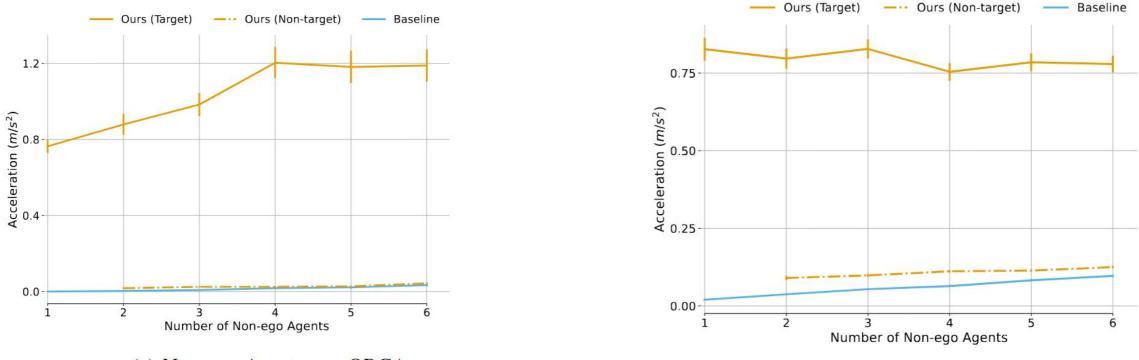


Fig. 7: The minimum distance between the target agent's ycoordinate and the top of the virtual goal line (SF - Social Force)



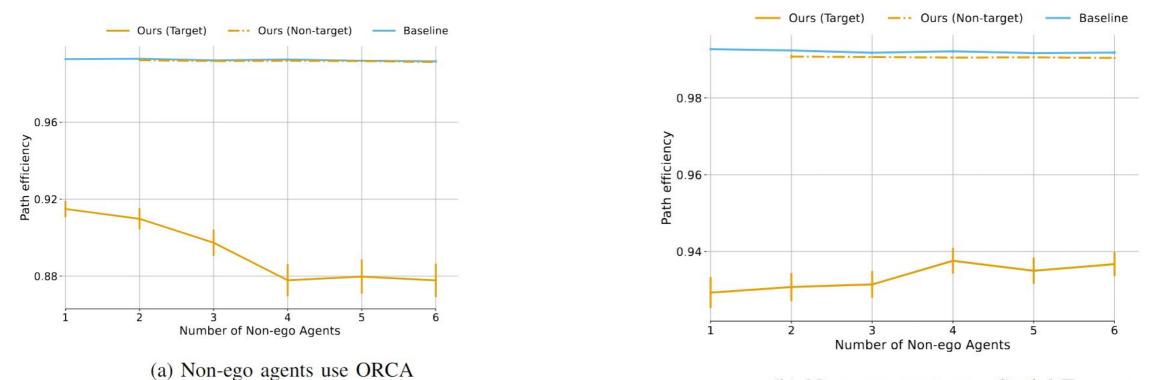


(a) Non-ego Agents use ORCA

(b) Non-ego Agents use Social Forces

Fig. 8: The average acceleration of the non-ego agents over their trajectories. (a) is the case when all non-ego agents use ORCA and (b) is the case when all non-ego agents use the social forces model





(b) Non-ego agents use Social Forces

Fig. 9: The path efficiency of the non-ego agents. (a) is the case when all non-ego agents use ORCA and (b) is the case when all non-ego agents use the social forces model



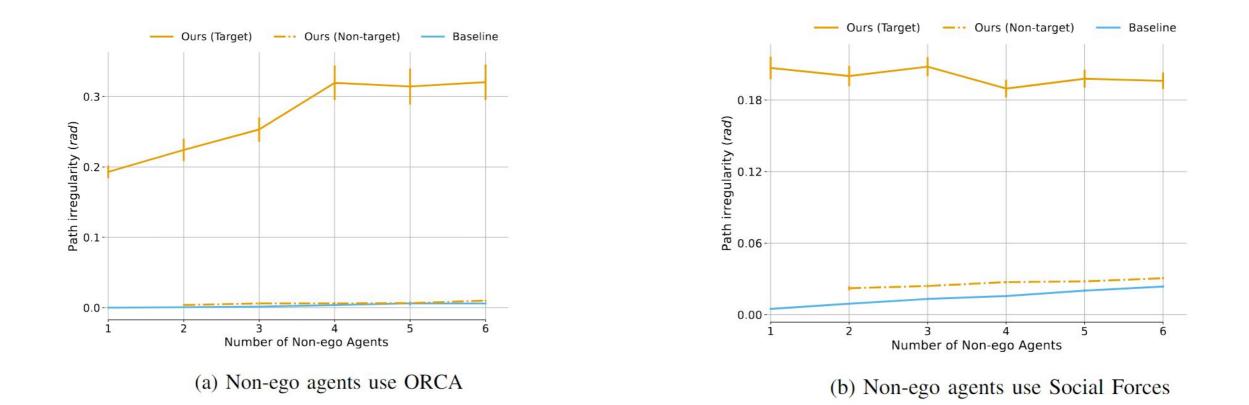
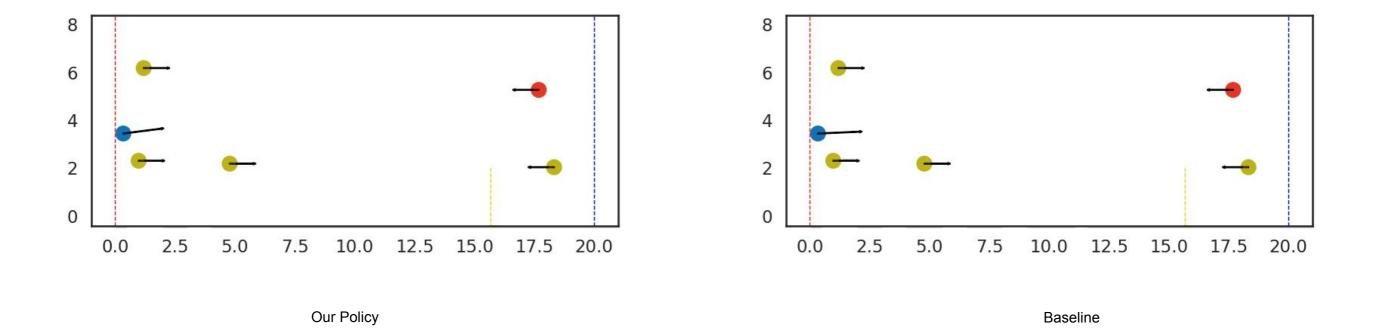


Fig. 10: The path irregularity of the non-ego agents. (a) is the case when all non-ego agents use ORCA and (b) is the case when all non-ego agents use the social forces model







- We proposed the I-ORCA algorithm that inverts ORCA to generate velocities for an agent to
  optimally nudge another agent in the desired direction
- We computed the nudge efficiency metric, which showed that "leading" the agent toward the desired direction is the best way to nudge it
- We proposed the smooth efficient nudge policy that utilizes this result to smoothly nudge the target agent toward the desired objective
- Our results indicate that an agent using our policy was able to implicitly nudge the target agent while not disturbing the other non-target agents in the scene
  - These results were generalizable across the ORCA and Social Forces motion models



- Highly sensitive to policy parameters
  - Future work could try online learning of parameters
- Cannot guarantee collision avoidance with target agent
- Not personalized
  - If other agents are humans, they could have their own policy parameters
- Setting the desired velocity
  - Can be set up as an optimization problem to minimize discomfort to the target agent
- Detecting impossible cases
- Incorporating learning of agents' goals



# THANK YOU, QUESTIONS?



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- 4. M. Kwon, M. Li, A. Bucquet, and D. Sadigh, "Influencing leading andfollowing in human-robot teams," in Proceedings of Robotics: Scienceand Systems, FreiburgimBreisgau, Germany, June 2019.
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